

Solve each equation for  $0^\circ \leq \theta < 360^\circ$ . Give answer to the nearest tenth of a degree.

1.  $2\cos^2\theta + 3\sin\theta - 3 = 0$

$$\begin{aligned} 2(1 - \sin^2\theta) + 3\sin\theta - 3 &= 0 \\ 2 - 2\sin^2\theta + 3\sin\theta - 3 &= 0 \\ -2\sin^2\theta + 3\sin\theta - 1 &= 0 \\ 2\sin^2\theta - 3\sin\theta + 1 &= 0 \\ (2\sin\theta - 1)(\sin\theta - 1) &= 0 \\ 2\sin\theta - 1 = 0 \quad \sin\theta - 1 = 0 \\ \sin\theta = \frac{1}{2} \quad \sin\theta = 1 \\ \theta = 30^\circ, 90^\circ, 150^\circ \end{aligned}$$

Simplify each expression.

3.  $\cot A(\sec A - \cos A)$

$$\begin{aligned} \frac{\cos A}{\sin A} \left( \frac{1}{\cos A} - \cos A \right) \\ = \frac{1}{\sin A} - \frac{\cos^2 A}{\sin A} \\ = \frac{1 - \cos^2 A}{\sin A} \\ = \frac{\sin^2 A}{\sin A} \\ = \sin A \end{aligned}$$

5.  $(\sec x + \tan x)(1 - \sin x)$  (FOIL!)

$$\begin{aligned} \sec x - \frac{\sin x}{\cos x} + \tan x - \frac{\sin^2 x}{\cos x} \\ = \frac{1}{\cos x} - \frac{\sin x}{\cos x} + \frac{\sin x}{\cos x} - \frac{\sin^2 x}{\cos x} \\ = \frac{1 - \sin^2 x}{\cos x} \\ = \frac{\cos^2 x}{\cos x} \\ = \cos x \end{aligned}$$

2.  $\cos\theta \cot\theta = 2\cos\theta$

$$\begin{aligned} \cos\theta \cot\theta - 2\cos\theta &= 0 \\ \cos\theta(\cot\theta - 2) &= 0 \\ \cos\theta = 0 \quad \cot\theta - 2 = 0 \\ \theta = 90^\circ, 270^\circ \quad \cot\theta = 2 \\ \tan\theta = \frac{1}{2} \\ \theta = \tan^{-1}\left(\frac{1}{2}\right) \\ \theta = 26.6^\circ, 206.6^\circ \\ \theta = 26.6^\circ, 90^\circ, 206.6^\circ, 270^\circ \end{aligned}$$

4.  $\frac{\cot\theta}{\sin(90^\circ - \theta)}$

$$\begin{aligned} \frac{\cot\theta}{\cos\theta} \\ \cot\theta \cdot \frac{1}{\cos\theta} \\ \frac{1}{\cos\theta} \cdot \frac{\cos\theta}{\sin\theta} \\ = \frac{1}{\sin\theta} = \csc\theta \end{aligned}$$

6.  $\frac{\cot x + \tan x}{\csc^2 x}$

$$\begin{aligned} \frac{1}{\csc^2 x} [\cot x + \tan x] \\ \sin^2 x \left[ \frac{\cos x}{\sin x} + \frac{\sin x}{\cos x} \right] \\ \frac{\sin x \cos x}{1} + \frac{\sin^3 x}{\cos x} \\ \frac{\sin x \cos^2 x}{\cos x} + \frac{\sin^3 x}{\cos x} \\ \frac{\sin x (\cos^2 x + \sin^2 x)}{\cos x} = \frac{\sin x}{\cos x} = \tan x \end{aligned}$$

Prove the given identity.

$$7. \frac{\cot A(1 + \tan^2 A)}{\tan A} = \csc^2 A$$

$$\frac{\cot A (\sec^2 A)}{\tan A}$$

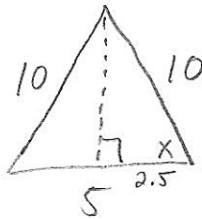
$$\frac{1}{\tan A} \cdot \cot A (\sec^2 A) = \csc^2 A$$

$$\cot^2 A (\sec^2 A) = \csc^2 A$$

$$\frac{\cos^2 A}{\sin^2 A} \cdot \frac{1}{\cos^2 A} = \csc^2 A$$

$$\frac{1}{\sin^2 A} = \csc^2 A$$

8. The sides of an isosceles triangle have lengths 5, 10, and 10. What are the measures of the angles?



$$\cos x^\circ = \frac{2.5}{10}$$

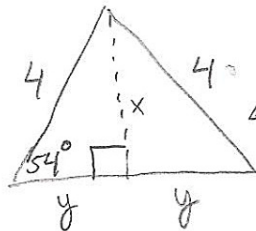
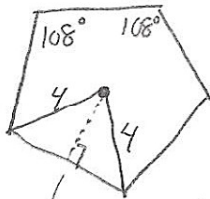
$$\cos x = \frac{1}{4}$$

$$x = \cos^{-1}\left(\frac{1}{4}\right)$$

$$x = 75.5^\circ$$

$$75.5^\circ, 75.5^\circ, \text{ and } 29^\circ$$

9. A regular pentagon is inscribed in a circle with a radius of 4 inches. Find the area of the pentagon.



$$A = \frac{1}{2}(4,7)(3,23)$$

$$A = 7.59 \text{ in}^2$$

$$\sin 54^\circ = \frac{x}{4}$$

$$x = 3.23$$

$$\cos 54^\circ = \frac{y}{4}$$

$$y = 2.35$$

There are 5  $\cong$   $\triangle$  so  
 $A = 5(7.59 \text{ in}^2)$   
 $A = 37.953 \text{ in}^2$