

2. Get the *general* solution by finding the argument.
  - a. If it is a *special* angle, write the *exact* value.
  - b. If *not*, use calculator or tables.
3. Do whatever algebra you need to find the *variable* in the argument (Examples 2, 3, 4, and 6).
4. Write the solution set.
  - a. Find all solutions in the domain by picking integer values of  $n$  in the general solution.
  - b. Check for extraneous solutions if you have multiplied by a variable.

The following exercise will give you practice solving trigonometric equations.

**EXERCISE 3-9**

For Problems 1 through 40, solve the equation in the indicated domain.

1.  $\tan \theta + \sqrt{3} = 0$ ,  $\theta \in [0^\circ, 360^\circ)$
2.  $2 \cos \theta + \sqrt{3} = 0$ ,  $\theta \in [0^\circ, 360^\circ)$
3.  $2 \sin(\theta + 47^\circ) = 1$ ,  $\theta \in [0^\circ, 360^\circ)$
4.  $\sec(\theta + 81^\circ) = 2$ ,  $\theta \in [0^\circ, 360^\circ)$
5.  $4 \cos^2 \theta = 1$ ,  $\theta \in [-180^\circ, 180^\circ]$
6.  $4 \sin^2 \theta = 3$ ,  $\theta \in [-180^\circ, 180^\circ]$
7.  $2 \sin \theta \cos \theta = \sqrt{2} \cos \theta$ ,  $\theta \in \{\text{real numbers of degrees}\}$
8.  $\tan \theta \sec \theta = \tan \theta$ ,  $\theta \in \{\text{real numbers of degrees}\}$
9.  $\tan x - \sqrt{3} = 2 \tan x$ ,  $x \in \{\text{real numbers}\}$
10.  $\cos x + 2 = 3 \cos x$ ,  $x \in \{\text{real numbers}\}$
11.  $2 \sin^2 \theta + \sin \theta = 0$ ,  $\theta \in (-180^\circ, 180^\circ)$
12.  $\tan^2 \theta + \tan \theta = 0$ ,  $\theta \in [-90^\circ, 90^\circ)$
13.  $2 \cos^2 x - 5 \cos x + 2 = 0$ ,  $x \in [0, 2\pi)$
14.  $2 \sec^2 x - 3 \sec x - 2 = 0$ ,  $x \in [0, 2\pi)$
15.  $\sin^2 \theta + 5 \sin \theta + 6 = 0$ ,  $\theta \in [0^\circ, 360^\circ)$
16.  $4 \csc^2 \theta + 4 \csc \theta + 1 = 0$ ,  $\theta \in [0^\circ, 360^\circ)$
17.  $\tan^2 x - \sec x - 1 = 0$ ,  $x \in [-\pi, \pi)$
18.  $3 - 3 \sin x - 2 \cos^2 x = 0$ ,  $x \in [-\pi, \pi]$
19.  $1 - \cos \theta = -\sin \theta$ ,  $\theta \in [-180^\circ, 180^\circ)$
20.  $\frac{1 + \cos \theta}{\sin \theta} = -1$ ,  $\theta \in [-180^\circ, 180^\circ)$
21.  $4 \sin x \cos x = \sqrt{3}$ ,  $x \in [0, 2\pi)$
22.  $\sin x = \sin 2x$ ,  $x \in [0, 2\pi)$
23.  $\frac{\sin(90^\circ - \theta)}{\sin \theta} = -\sqrt{3}$ ,  $\theta \in (-270^\circ, 270^\circ)$
24.  $\tan(90^\circ - \theta) = -1$ ,  $\theta \in (-180^\circ, 180^\circ)$
25.  $\sin 2\theta \cos 64^\circ + \cos 2\theta \sin 64^\circ = \frac{\sqrt{3}}{2}$ ,  $\theta \in [0^\circ, 360^\circ)$
26.  $\cos 3\theta \cos 12^\circ - \sin 3\theta \sin 12^\circ = \frac{1}{2}$ ,  $\theta \in [-120^\circ, 120^\circ)$
27.  $\cos 4\theta - \sin 2\theta = 0$ ,  $\theta \in (-90^\circ, 90^\circ)$
28.  $\cos 4\theta - \sin 2\theta = 1$ ,  $\theta \in [-90^\circ, 90^\circ)$
29.  $\cos 3\theta + \cos 5\theta = 0$ ,  $\theta \in (-90^\circ, 90^\circ)$
30.  $\sin 5\theta + \sin 7\theta = 0$ ,  $\theta \in [-90^\circ, 90^\circ)$
31.  $\cos x - \sqrt{3} \sin x = 1$ ,  $x \in (0, 2\pi]$
32.  $\sin x - \sqrt{3} \cos x = 1$ ,  $x \in [-\pi, \pi]$
33.  $\frac{\tan 10\theta + \tan 50^\circ}{1 - \tan 10\theta \tan 50^\circ} = \frac{\sqrt{3}}{3}$ ,  $\theta \in (0^\circ, 90^\circ)$
34.  $\tan \theta - \tan 10^\circ = 1 + \tan \theta \tan 10^\circ$ ,  $\theta \in [-180^\circ, 180^\circ]$
35.  $\tan \frac{1}{2}x + 1 = \cos x$ ,  $x \in [0, 4\pi]$
36.  $2 \cos^2 \frac{1}{2}x - 2 = 2 \cos x$ ,  $x \in [-\pi, \pi]$
37.  $2 \cos(\theta + 30^\circ) \cos(\theta - 30^\circ) = 1$ ,  $\theta \in [-180^\circ, 180^\circ]$
38.  $4 \sin(\theta + 75^\circ) \cos(\theta - 75^\circ) = 1$ ,  $\theta \in [-180^\circ, 180^\circ]$