

M1T1 (extra) Notes: Exact Circles

The only way for a calculation involving π to remain exact is to not use an approximation. But how can we represent all the digits of π if it goes on forever?

- Use the π symbol itself and leave it in your answer

It's a little awkward, but it has definite uses.

* do all the math around the π symbol. Leave the π symbol (like a variable) in your answer

Calculate the exact area (a) and circumference (b) of each circle:

1) radius = 8 inches

a) $A = \pi r^2$

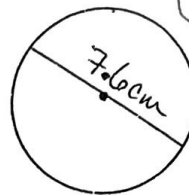
$A = 8^2 \pi$

$A = 64 \pi \text{ in}^2$

b) $C = 2\pi \cdot 8$

$C = 16 \pi \text{ in}$

2)



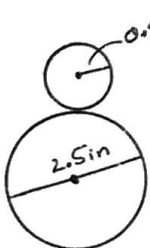
$r = 3.8$

a) $A = 3.8^2 \pi$

$A = 14.44 \pi \text{ cm}^2$

b) $C = 7.6 \pi \text{ cm}$

3) Composite Circumference Problem - way easier to just treat π as a variable at first
Calculate the TOTAL CIRCUMFERENCE



$5\pi + 10\pi$
 $2 \cdot \pi \cdot 0.5 + \pi \cdot 2.5$

$1\pi + 2.5\pi$

3.5π → now solve

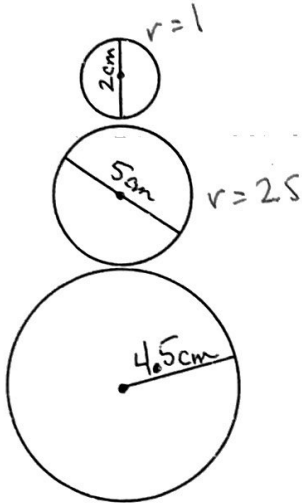
$10.9955 \dots$

$11.0 \text{ in} \approx C$

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4) Composite Area Problem - treat π as a variable, then bring in approximation at end

CALCULATE THE TOTAL AREA



$$5\pi + 12.5\pi + 20.25\pi$$

$$\pi \cdot 1^2 + \pi \cdot 2.5^2 + \pi \cdot 4.5^2$$

$$1\pi + 6.25\pi + 20.25\pi$$

$$27.5\pi$$

$$86.393$$

$$A \approx 86.4 \text{ cm}^2$$